

Product of Powers

Power of a Power

Power of a Product

Negative Exponent

Zero Exponent

Quotient of Powers

Power of a Quotient

Examples with Multiple Properties

1. $\frac{(x^3 y^2)^3}{x^{15} y^8}$

$$\frac{x^{15} y^6}{x^{15} y^8} = x^{15-15} y^{6-8} = y^{-2} = \frac{1}{y^2}$$

2. $\left(\frac{a^{-4}}{b^2}\right)^2$

$$\frac{a^{-4 \cdot 2}}{b^{2 \cdot 2}} = \frac{a^{-8}}{b^4} = \frac{1}{a^8 b^4}$$

3. $\left(\frac{-2a^2 b^3}{a^5 b^3}\right)^3$

$$\frac{-2^3 a^{2 \cdot 3} b^{3 \cdot 3}}{a^{5 \cdot 3} b^{3 \cdot 3}} = \frac{-8 a^6 b^9}{a^{15} b^9} = \frac{-8 a^{6-15}}{a^9} = \frac{-8 a^{-9}}{a^9} = \frac{-8}{a^9}$$

Scientific Notation: $a \times 10^b$
between 1 & 10, $\neq 10$

- Negative exponent \leftarrow move the decimal
- Positive exponent \rightarrow move the decimal

Operations with Scientific Notation:

Multiply:

$$85,000,000 \times 1200$$
$$(8.5 \times 10^7)(1.2 \times 10^3)$$
$$10.2 \times 10^{10}$$
$$\boxed{1.02 \times 10^{11}}$$

Divide:

$$\frac{1.1 \times 10^{-3}}{5.5 \times 10^{-8}}$$
$$.2 \times 10^5$$
$$\boxed{2 \times 10^4}$$

$$a^m \cdot a^n = \underline{a^{m+n}}$$

$$2^3 \cdot 2^4 = 2^7$$

$$(a^m)^n = \underline{a^{mn}}$$

$$(5^2)^6 = 5^{12}$$
$$5^2 \cdot 5^2 \cdot 5^2 \cdot 5^2 \cdot 5^2 \cdot 5^2$$

$$(a \cdot b)^m = \underline{a^m b^m}$$

$$(3x^2)^4 = 3^4 x^8$$

$$a^{-m} = \underline{\frac{1}{a^m}} \quad a \neq 0$$

$$4^{-2} = \frac{1}{4^2} = \frac{1}{16}$$

$$\frac{1}{a^{-m}} = \underline{a^m}$$

$$\frac{1}{4^{-2}} = 4^2 = 16$$

$$a^0 = \underline{1} \quad a \neq 0$$

$$(5x^2y^3z^1)^0 = 1$$

$$\frac{a^m}{a^n} = \underline{a^{m-n}} \quad a \neq 0$$

$$\frac{2^3}{2^2} = 2^{3-2} = 2^1 = 2$$

$$\left(\frac{a}{b}\right)^m = \underline{\frac{a^m}{b^m}} \quad b \neq 0$$

$$\left(\frac{3}{2}\right)^4 = \frac{3^4}{2^4}$$