

Learning Target(s): I can use deductive reasoning to write an algebraic proof.
 I can identify the reflexive, symmetric, and transitive properties.

Notes: 2.5 Reason Using Properties from Algebra

ALGEBRAIC PROPERTIES OF EQUALITY

Let a , b and c be real numbers.

Addition Property If $a = b$, then $a + c = b + c$

Subtraction Property If $a = b$, then $a - c = b - c$

Multiplication Property If $a = b$, then $ac = bc$

Division Property If $a = b$ and $c \neq 0$, then $\frac{a}{c} = \frac{b}{c}$

Substitution Property If $a = b$, then a can be substituted
for b in any equation or expression

Ex. 1
Solve $2x + 3 = 9 - x$. Write a reason for each step.

Equation

$$\begin{array}{r} 2x + 3 = 9 - x \\ + x \qquad \qquad + x \\ \hline \end{array}$$

Explanation
original equation
add x to each side

Reason
Given
Add. Prop.

$$\begin{array}{r} 3x + 3 = 9 \\ -3 \quad -3 \\ \hline \end{array}$$

subtract 3 from both sides

Subtraction Prop
Subt.

$$\begin{array}{r} 3x = 6 \\ \frac{3x}{3} = \frac{6}{3} \end{array}$$

divide both sides by 3

Div. Prop

$$x = 2$$

Distributive Property

$a(b + c) =$ $ab + ac$, where a , b , and c are real numbers.

Ex. 2

Solve $-4(6x + 2) = 64$. Write a reason for each step.

Equation
$-4(6x + 2) = 64$
$-24x - 8 = 64$
$\quad + 8 \quad + 8$
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$-24x = 72$
$\quad -24 \quad -24$
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$x = -3$

Explanation
original equation
Distribute -4
Add 8 to each side
Divide both sides by -24

Reason
Given
Dist. Prop.
Add. Prop.
Div. Prop.

Try it!

1. Solve $x - 5 = 7 + 2x$. Write a reason for each step.

Equation

Explanation

Reason

2. Solve $4(5 - x) = -2x$. Write a reason for each step.

Equation

Explanation

Reason